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## Coherence order and coherence selection

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### Outline

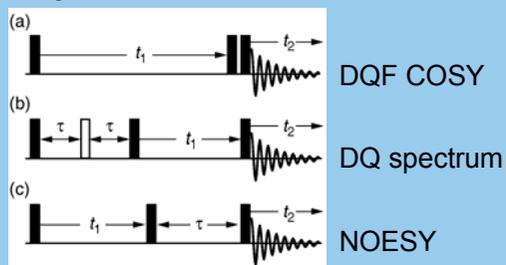
- Why we need coherence selection
- Concept of coherence order
- Coherence transfer pathways (CTPs)
- Selecting a CTP with phase cycling
- Selecting a CTP with gradients
- Biomolecular NMR (time permitting)

### Further information

- PDF of these slides will be available on the CCPN website
- See also:  
*Understanding NMR Spectroscopy*, James Keeler (Wiley) [Chapt. 11]

*Spin Dynamics. Basics of Nuclear Magnetic Resonance*, Malcolm Levitt (Wiley)

### Why we need coherence selection



The spins don't know what we want!  
We want one out of many possibilities

### Coherence order, $p$

Defined by phase acquired during rotation by about  $z$

$$\hat{\rho}^{(p)} \xrightarrow{\text{rotate by } \varphi \text{ about } z} \hat{\rho}^{(p)} \times \exp(-ip\varphi)$$

phase acquired is  $-p\varphi$

different  $p$  separated by using this property

### Properties of coherence order

- takes values 0,  $\pm 1$ ,  $\pm 2$  ...
  - 0 is z-magnetization,
  - $\pm 1$  is single quantum,
  - $\pm 2$  is double quantum etc.
- only  $p = -1$  is observable
- maximum/minimum value is  $\pm N$ , where  $N$  is number of spins

### Effect of pulses

$p \xrightarrow{\text{RF pulse}} \text{all possible values of } p$

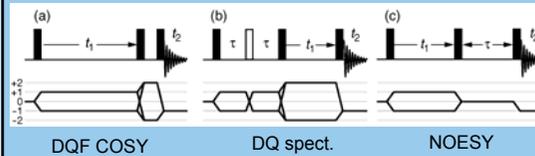
- which is why we need selection

special case:

$p \xrightarrow{180^\circ \text{ pulse}} -p$

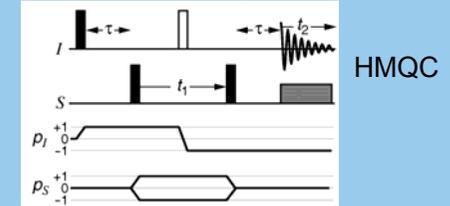
### Coherence transfer pathway (CTP)

Indicates the *desired* coherence order at each point



note: always starts at  $p = 0$   
always ends at  $p = -1$

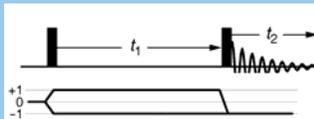
### Heteronuclear experiments



separate  $p$  for each nucleus ( $p_I, p_S$ )  
ends with  $p = -1$  on *observed* nucleus  
pulse to S only affects  $p_S$

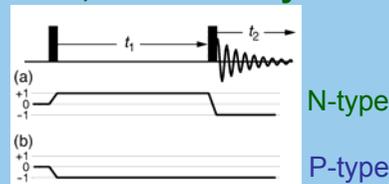
### Frequency discrimination and lineshapes in 2D

for absorption mode spectra must retain  $p = \pm 1$  during  $t_1$ : *symmetrical pathways*



combine this with frequency discrimination using 'TPPI' or 'States'

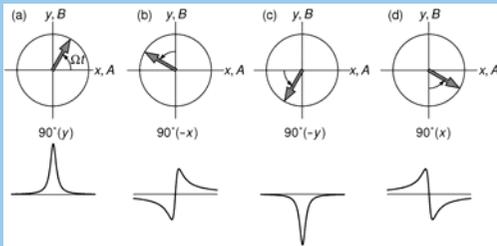
### - or, alternatively



1. record two *separate* spectra:  
echo or N-type:  $p = +1$  during  $t_1$   
anti-echo or P-type:  $p = -1$  during  $t_1$
2. combine to give absorption spectrum

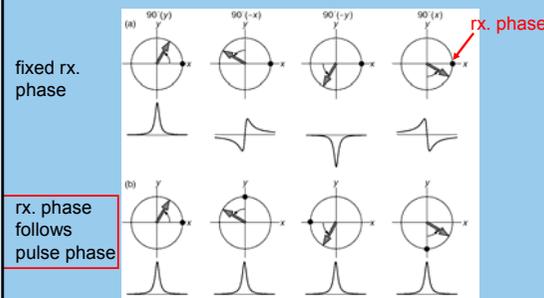
### Phase cycling

### Pulse phase



the phase of the spectrum depends on the phase of the pulse

### Receiver (rx.) phase



fixed rx. phase

rx. phase follows pulse phase

### Receiver phase

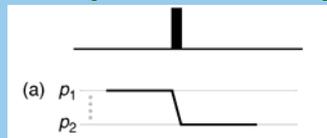
If the signal generated by the pulse sequence shifts in phase, then this can always be compensated for by shifting the receiver by the same amount.

### Phase cycling

Selection of a pathway by repeating the sequence with a systematic variation of the pulse and rx. phases

How to design the sequence of phases, - the *phase cycle*?

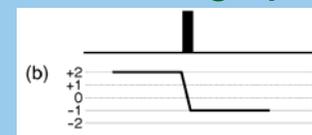
### Effect of phase shift of pulse



Pulse causes transfer from  $p_1$  to  $p_2$   
 Change in coherence order  $\Delta\rho = p_2 - p_1$   
 If pulse phase shifted by  $\Delta\phi$  phase acquired by signal is

$$-\Delta\rho \times \Delta\phi$$

### Selection of a single pathway



+2 to -1, so  $\Delta\rho = -1 - (+2) = -3$

phase acquired by signal when pulse shifted by  $\Delta\phi$  is

$$-\Delta\rho \times \Delta\phi = 3 \Delta\phi$$

### Four-step cycle

step	pulse $\Delta\phi$	$3 \Delta\phi$	equiv( $3 \Delta\phi$ )
1	$0^\circ$		
2	$90^\circ$		
3	$180^\circ$		
4	$270^\circ$		

### Four-step cycle

step	pulse $\Delta\phi$	$3 \Delta\phi$	equiv( $3 \Delta\phi$ )
1	$0^\circ$	$0^\circ$	
2	$90^\circ$	$270^\circ$	
3	$180^\circ$	$540^\circ$	
4	$270^\circ$	$810^\circ$	

### Four-step cycle

step	pulse $\Delta\phi$	$3 \Delta\phi$	equiv( $3 \Delta\phi$ )
1	$0^\circ$	$0^\circ$	$0^\circ$
2	$90^\circ$	$270^\circ$	$270^\circ$
3	$180^\circ$	$540^\circ$	$180^\circ$
4	$270^\circ$	$810^\circ$	$90^\circ$

### Four-step cycle

Pulse goes  
 $[0^\circ, 90^\circ, 180^\circ, 270^\circ]$

Pathway with  $\Delta p = -3$  acquires phase  
 $[0^\circ, 270^\circ, 180^\circ, 90^\circ]$

If receiver phase follows these phases,  
 contribution from the pathway will add up

- but what about other pathways?

### - other pathways

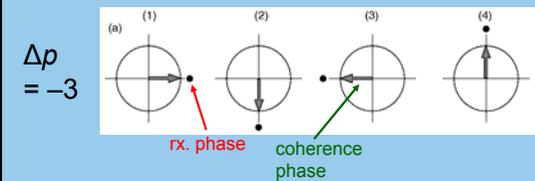
e.g.  $\Delta p = -2$  so  $-\Delta p \times \Delta\phi = 2 \Delta\phi$

step	pulse $\Delta\phi$	$2 \Delta\phi$	equiv( $2 \Delta\phi$ )
1	$0^\circ$	$0^\circ$	$0^\circ$
2	$90^\circ$	$180^\circ$	$180^\circ$
3	$180^\circ$	$360^\circ$	$0^\circ$
4	$270^\circ$	$540^\circ$	$180^\circ$

Selected with rx. phases  
 $[0^\circ, 270^\circ, 180^\circ, 90^\circ]$  ?

### Selected pathways

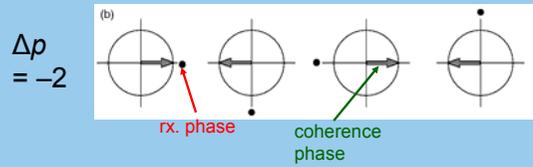
rx. phase  $[0^\circ, 270^\circ, 180^\circ, 90^\circ]$



For  $\Delta p = -3$ , rx. phase follows coherence phase: all four steps add up

### Selected pathways

rx. phase [0°, 270°, 180°, 90°]



For  $\Delta p = -2$ , signal cancels on four steps

### Selectivity

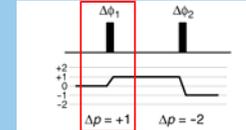
A **four-step** cycle designed to select a particular value of  $\Delta p$  will also select  $\Delta p + 4, \Delta p + 8 \dots$  and  $\Delta p - 4, \Delta p - 8 \dots$

- all other pathways are suppressed

(-4) **-3** (-2) (-1) (0) **1** (2) (3) (4) **5**

selected in **bold**, suppressed in ( )

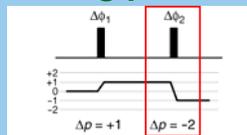
### Combining phase cycles



four-step cycle to select  $\Delta p = +1$

step	pulse $\Delta\phi_1$	$-\Delta\phi_1$	equiv( $-\Delta\phi_1$ )
1	0°	0°	0°
2	90°	-90°	270°
3	180°	-180°	180°
4	270°	-270°	90°

### Combining phase cycles



four-step cycle to select  $\Delta p = -2$

step	pulse $\Delta\phi_2$	$2\Delta\phi_2$	equiv( $-\Delta\phi_2$ )
1	0°	0°	0°
2	90°	180°	180°
3	180°	360°	0°
4	270°	540°	180°

### Complete both cycles independently

step	$\Delta\phi_1$	$-\Delta\phi_1$	equiv( $-\Delta\phi_1$ )	$\Delta\phi_2$	$2\Delta\phi_2$	equiv( $2\Delta\phi_2$ )	total
1	0°	0°	0°	0°	0°	0°	0°
2	90°	-90°	270°	0°	0°	0°	270°
3	180°	-180°	180°	0°	0°	0°	180°
4	270°	-270°	90°	0°	0°	0°	90°
5	0°	0°	0°	90°	180°	180°	180°
6	90°	-90°	270°	90°	180°	180°	90°
7	180°	-180°	180°	90°	180°	180°	0°
8	270°	-270°	90°	90°	180°	180°	270°
9	0°	0°	0°	180°	360°	0°	0°
10	90°	-90°	270°	180°	360°	0°	270°
11	180°	-180°	180°	180°	360°	0°	180°
12	270°	-270°	90°	180°	360°	0°	90°
13	0°	0°	0°	270°	540°	180°	180°
14	90°	-90°	270°	270°	540°	180°	90°
15	180°	-180°	180°	270°	540°	180°	0°
16	270°	-270°	90°	270°	540°	180°	270°

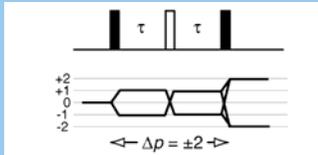
### Tricks: 1

1. The first pulse can *only* generate  $p = \pm 1$  from equilibrium magnetization

- no need to phase cycle this pulse

### Tricks: 2

2. Group pulses together and cycle as a unit



All pulses:  $[0^\circ, 90^\circ, 180^\circ, 270^\circ]$

Rx. for  $\Delta p = \pm 2$ :  $[0^\circ, 180^\circ, 0^\circ, 180^\circ]$

### Tricks: 3

3. Only  $p = -1$  is observable, so it does not matter if other values of  $p$  are generated by the *last pulse*

- no need to phase cycle the *last pulse*, if a coherence order has been selected unambiguously *before* this pulse

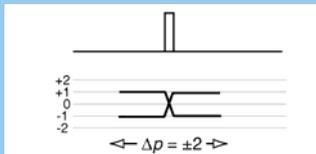
### Tricks: 4

4. Don't worry about high orders of multiple quantum coherence e.g  $\geq 4$ .

- they are hard to generate and likely to give weak signals, especially if the lines are broad

### Refocusing pulses: EXORCYCLE

Refocusing pulses cause  $p \rightarrow -p$



e.g.  $\Delta p = \pm 2$   
(single quantum)

Pulse:  $[0^\circ, 90^\circ, 180^\circ, 270^\circ]$

Rx. for  $\Delta p = \pm 2$ :  $[0^\circ, 180^\circ, 0^\circ, 180^\circ]$

### Axial peak suppression

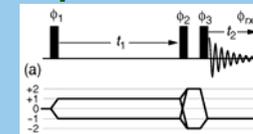
z-magnetization which recovers by relaxation during a pulse sequence is made observable by last pulse

- leads to peaks at  $\omega_1=0$ : **axial peaks**  
- easily suppressed using a two-step cycle

1<sup>st</sup> pulse:  $[0^\circ, 180^\circ]$

Rx. for  $\Delta p = \pm 1$ :  $[0^\circ, 180^\circ]$

### Examples: DQF COSY



symmetrical pathways in  $t_1$

final pulse has  $\Delta p = -3$  and  $+1$

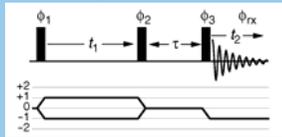
- select using four-step cycle:

$\Phi_3 = [0^\circ, 90^\circ, 180^\circ, 270^\circ]$

$\Phi_{rx} = [0^\circ, 270^\circ, 180^\circ, 90^\circ]$

this is sufficient, as  $p$  can only be  $\pm 1$  in  $t_1$

### Examples: NOESY



symmetrical pathways in  $t_1$

final pulse has  $\Delta p = -1$

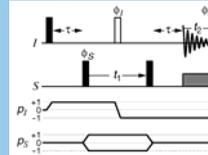
- select using four-step cycle:

$\phi_3 = [0^\circ, 90^\circ, 180^\circ, 270^\circ]$

$\phi_{rx} = [0^\circ, 90^\circ, 180^\circ, 270^\circ]$

this is sufficient, as  $p$  can only be  $\pm 1$  in  $t_1$

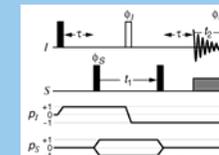
### Examples: HMQC



select  $\Delta p_S = \pm 1$  at first S pulse  
and  $\Delta p_I = \pm 2$  at  $180^\circ$  I pulse

step	1	2	3	4	5	6	7	8
$\Phi_S$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$
$\Phi_I$	$0^\circ$	$0^\circ$	$90^\circ$	$90^\circ$	$180^\circ$	$180^\circ$	$270^\circ$	$270^\circ$
$\Phi_{rx}$	$0^\circ$	$180^\circ$	$180^\circ$	$0^\circ$	$0^\circ$	$180^\circ$	$180^\circ$	$0^\circ$

### Difference spectroscopy: HMQC



The cycle  $[0^\circ, 180^\circ]$  on first S pulse and rx. is just **difference spectroscopy**:

selects that part of the signal which goes via the S spin

### Difference spectroscopy

In heteronuclear experiments, a simple two-step phase cycle (+x/-x) on the pulse causing the transfer often suffices

- this is simply difference spectroscopy

### Problems with phase cycling

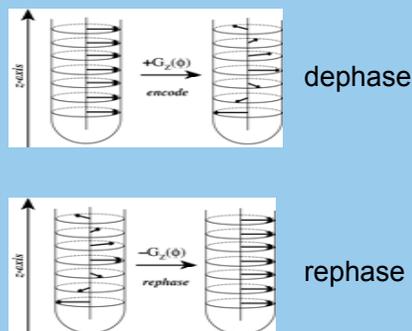
- phase cycle must be completed:
  - unacceptably long experiment, especially for 2D/3D
- cancellation of unwanted signals may be imperfect (especially for proton detected experiments)

### Gradient pulses

### Field gradient pulses

- the  $B_0$  field is made inhomogeneous for a short period (few ms)
- coherences dephase, all signal lost
- a subsequent gradient may rephase some of the coherences

### Dephasing and rephasing



### Spatially dependent phase

phase acquired by coherence  $p$  at position  $z$  in sample, after time  $t$

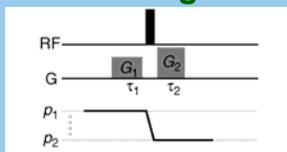
$$\varphi(z) = -p \times \gamma G z t$$

gyromagnetic ratio

gradient strength,  $G \text{ cm}^{-1}$

**phase depends on position and  $p$**

### Selection with a gradient pair

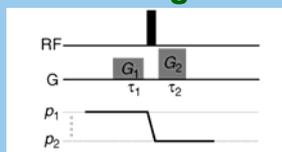


phase due to  $G_1$ :  $\varphi_1(z) = -p_1 \times \gamma G_1 z \tau_1$

phase due to  $G_2$ :  $\varphi_2(z) = -p_2 \times \gamma G_2 z \tau_2$

refocusing condition:  $\varphi_1(z) + \varphi_2(z) = 0$

### Selection with a gradient pair



$$\varphi_1(z) + \varphi_2(z) = -p_1 \gamma G_1 z \tau_1 - p_2 \gamma G_2 z \tau_2 = 0$$

$$\frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{p_2}{p_1}$$

can alter sign of  $G$

### Selection with a gradient pair

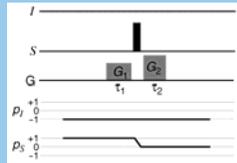


$$\frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{p_2}{p_1}$$

e.g.  $p_1 = +2, p_2 = -1 \rightarrow \frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{-1}{+2} = \frac{1}{2}$

alternatives  $\left\{ \begin{array}{l} \text{if } G_1 = G_2, \tau_2 = 2 \tau_1 \\ \text{if } \tau_1 = \tau_2, G_2 = 2 G_1 \end{array} \right.$

### Heteronuclear case



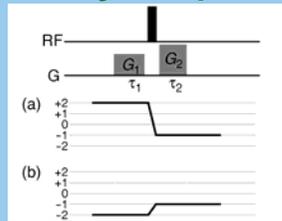
only  $p_S$  changes

$$\varphi_1(z) = -(p_I \gamma_I + p_S \gamma_S) G_1 z \tau_1 = -(-\gamma_I + \gamma_S) G_1 z \tau_1$$

$$\varphi_2(z) = -(p_I \gamma_I + p_S \gamma_S) G_2 z \tau_2 = -(-\gamma_I - 0) G_2 z \tau_2$$

$$\frac{G_1 \tau_1}{G_2 \tau_2} = \frac{1}{(\gamma_S / \gamma_I) - 1}$$

### Only one pathway selected

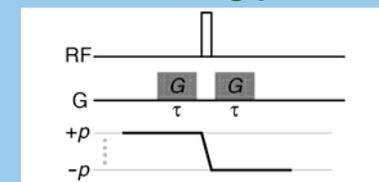


$$\frac{G_1 \tau_1}{G_2 \tau_2} = \frac{1}{2}$$

$$\frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{1}{2}$$

can only select *one* of these pathways  
 - potential loss of sensitivity  
 - problems in two-dimensional NMR

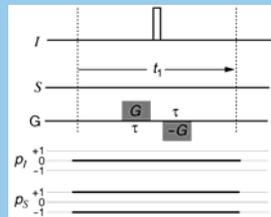
### Refocusing pulses



Ideal 180° causes  $p \rightarrow -p$

Selected for *all*  $p$  by equal gradients  
 - 'cleans up' imperfect 180°

### 180° in heteronuclear case

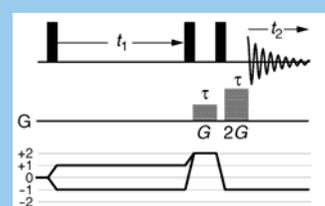


no coherence on  $I$  spin

180° to  $I$  is acting as *inversion pulse*

Gradient pair 'cleans up' imperfect 180°  
 - leaves  $S$  spin coherences unaffected

### Phase errors

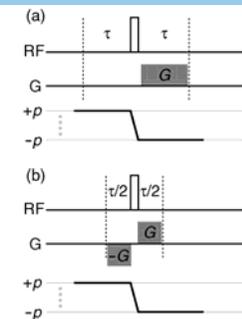


DQF COSY

Offsets continue to evolve during gradients  
 - results in severe frequency-dependent phase errors

### Avoiding phase errors

add refocusing pulse / use an existing one



offset evolution refocused by 180° pulse

more time efficient alternative

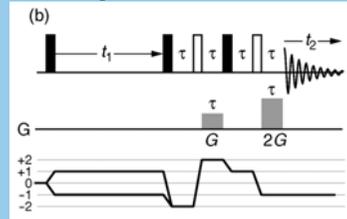
## Selection of z-magnetization

A gradient dephases all\* coherences:  
 - leaves behind only z-magnetization  
 - simple and convenient

called a *purge gradient* or *homospoil*

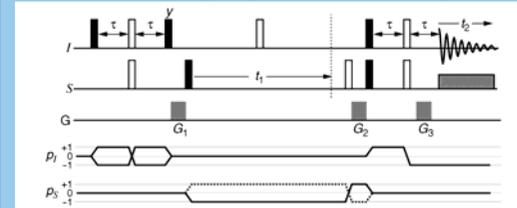
\*except homonuclear zero-quantum

## Examples: DQF COSY



- symmetrical pathways in  $t_1$  (no gradient)
- extra  $180^\circ$  pulses to avoid phase errors
- loss of sensitivity

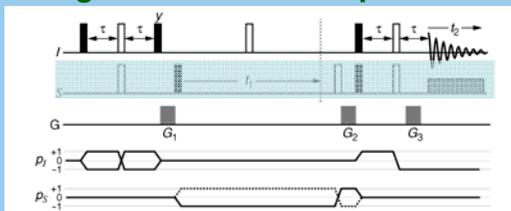
## HSQC (separate P-/N-)



- $G_1$  is purge gradient
- extra  $180^\circ$  associated with  $G_2$
- $G_3$  in existing spin echo

$$G_2\tau_2/G_3\tau_3 = \pm \gamma_I/\gamma_S$$

## Suppression of I/spin magnetization not coupled to S



- I magnetization dephased by  $G_1$
- choose  $G_2$  and  $G_3$  to avoid rephasing
- can omit  $G_2$  and  $G_3$  for labelled samples

## Advantages and disadvantages

- + minimizes experiment time
- + excellent suppression, especially in heteronuclear experiments with  $^1\text{H}$  obs.
- cannot select more than one pathway  
 → possible loss of SNR  
 → obtaining pure phase more complex
- phase errors  
 → requires elaboration of sequence
- loss due to diffusion

## Biomolecular NMR

(thanks to Daniel Nietlispach)

### Biomolecular NMR

- elaborate 2D and 3D experiments
- sensitivity at a premium
- long phase cycles unacceptable
  - as have to record many increments
- $^{13}\text{C}/^{15}\text{N}$  labelled samples
  - suppression not too difficult
- samples in  $\text{H}_2\text{O}$ 
  - water suppression vital
  - need to consider exchange
  - need to consider radiation damping

### INEPT transfers

most experiments are a series of (INEPT) transfers between different (types of) nuclei



can select each step using a simple two-step cycle (difference spectroscopy)

$$\varphi_1 = [0^\circ, 180^\circ] \quad \varphi_{rx} = [0^\circ, 180^\circ]$$

$$\text{or: } \varphi_1 = [x, -x] \quad \varphi_{rx} = [x, -x]$$

### INEPT transfers ... cont.

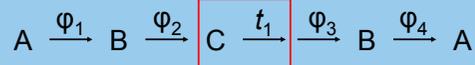


selecting each step would result in an excessively long phase cycle

but:

sequence 'directs' the transfers  
so selection on *final* step *may* be sufficient

### INEPT transfers ... cont.

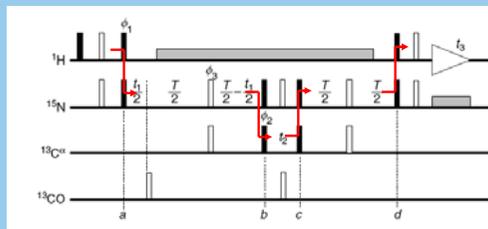


evolution in  $t_1$  critical to form of spectrum

may be advisable to select just prior to  $t_1$

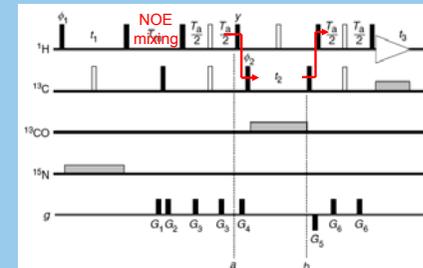
$$\text{i.e. } \varphi_2 = [x, -x] \quad \varphi_{rx} = [x, -x]$$

### Constant-time HNCA



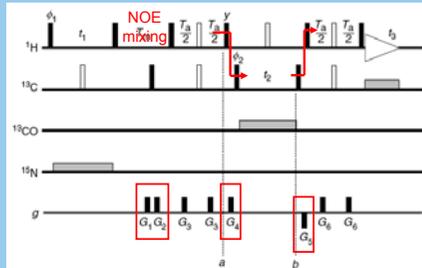
1.  $\varphi_1 = [y, -y]$  (prior to  $t_1$  + water suppression)
2.  $\varphi_2 = [x, x, -x, -x]$  (prior to  $t_2$ )
3. EXORCYCLE on  $\varphi_3$  (pulse in  $t_1$ )

### NOESY-HSQC



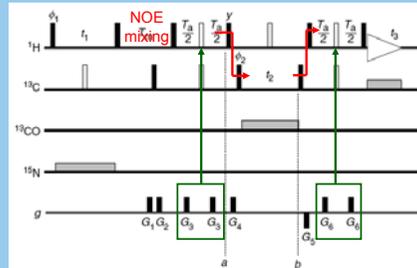
1.  $\varphi_1 = [x, -x]$  (axial peak suppression - vital)
2.  $\varphi_2 = [x, x, -x, -x]$  (prior to  $t_2$ )

### NOESY-HSQC



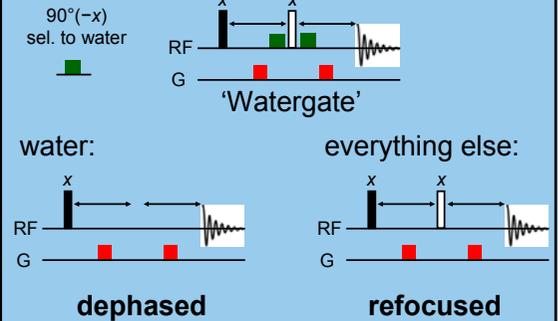
purging gradients – suppress everything that is not along z

### NOESY-HSQC



gradient pairs to remove signals arising from imperfect  $180^\circ$  refocusing pulses

### Water suppression using gradients



### Effect of exchange: 1

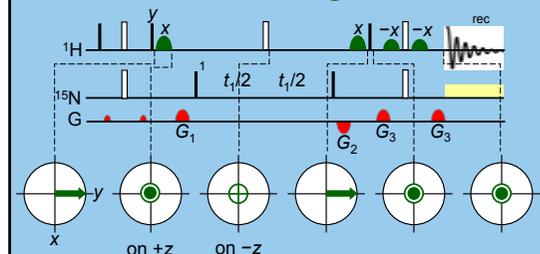
- dephasing the water sets its z-magn. to zero: *saturation*
- subsequent exchange of e.g. NH with saturated water will:
  - (1) transfer saturation
  - (2) slow-up return to equilibrium

Can lead to significant loss of sensitivity

### Effect of exchange: 2

- In contrast, if water is on +z (near to equilibrium), exchange will hasten return of NH to equilibrium
- 'Water flip back':
- keep water on +z as much as possible
  - avoid saturation of water

### zz-HSQC with flip-back and Watergate

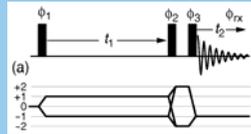


sel.  $90^\circ$  pulses used to keep water on +z (phase of  $^1\text{H}$  pulses fixed)

# THE END

Phew!

## DQF COSY (alternative)



symmetrical pathways in  $t_2$

group first two pulses and select  $\Delta p = \pm 2$

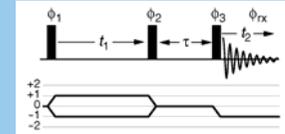
- select using four-step cycle:

$$\phi_1 \text{ and } \phi_2 = [0^\circ, 90^\circ, 180^\circ, 270^\circ]$$

$$\phi_{rx} = [0^\circ, 180^\circ, 0^\circ, 180^\circ]$$

this is sufficient, as  $p$  can only be  $-1$  in  $t_2$

## Examples: NOESY

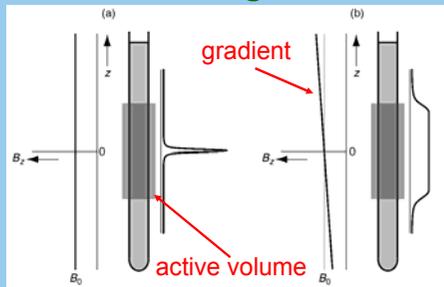


axial peak suppression also required

$$\phi_1 = [0^\circ, 180^\circ] \quad \phi_{rx} = [0^\circ, 180^\circ]$$

Step	1	2	3	4	5	6	7	8
$\Phi_1$	$0^\circ$	$0^\circ$	$0^\circ$	$0^\circ$	$180^\circ$	$180^\circ$	$180^\circ$	$180^\circ$
$\Phi_3$	$0^\circ$	$90^\circ$	$180^\circ$	$270^\circ$	$0^\circ$	$90^\circ$	$180^\circ$	$270^\circ$
$\Phi_{rx}$	$0^\circ$	$90^\circ$	$180^\circ$	$270^\circ$	$180^\circ$	$270^\circ$	$0^\circ$	$90^\circ$

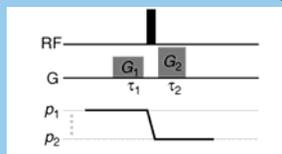
## Effect of a gradient



off: sharp line

on: v. broad line

## Selection with a gradient pair



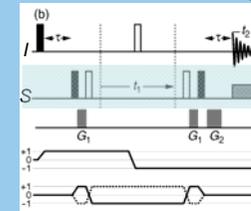
$$\frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{p_2}{p_1}$$

e.g.  $p_1 = -2, p_2 = -1 \rightarrow \frac{G_1 \tau_1}{G_2 \tau_2} = -\frac{-1}{-2} = -\frac{1}{2}$

refocusing:  $\tau_1 = \tau_2, G_2 = -2 G_1$

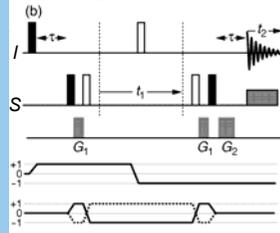
'-G' means opposite sense of gradient

## HMQC: suppression of I spin magnetization not coupled to S



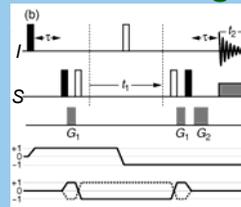
• I magnetization dephased by 1<sup>st</sup>  $G_1$ , but rephased by second  $G_1$ , and then dephased by  $G_2$

### Examples: HMQC



- separate expts. for P- and N-type
- additional 180° associated with both G<sub>1</sub>
- G<sub>2</sub> in existing delay, so no phase error

### HMQC: refocusing condition



P-type  
(solid line)

$$(-\gamma_I G_1 z \tau_1 - \gamma_S G_1 z \tau_1) + (\gamma_I G_1 z \tau_1 - \gamma_S G_1 z \tau_1) + (\gamma_I G_2 z \tau_2) = 0$$

$$-2\gamma_S G_1 z \tau_1 + \gamma_I G_2 z \tau_2 = 0$$

$$\frac{G_1 \tau_1}{G_2 \tau_2} = \frac{\gamma_I}{2\gamma_S}$$

### Reduced phase cycles

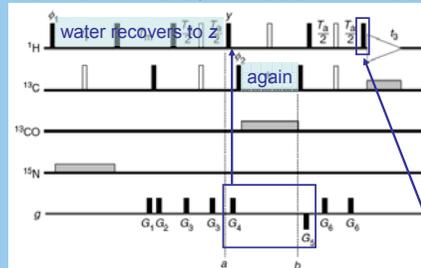
- imperfect 180° refocusing pulses often a source of unwanted signals
- EXORCYCLE (4 steps) will remove these
- may be able to use a shorter cycle

option 1: 180 = [x, -x]    rx = [x, x]  
selects p = 0, ±2

option 2: 180 = [x, y]    rx = [x, -x]  
selects ?

4-51

### NOESY-HSQC: fate of water



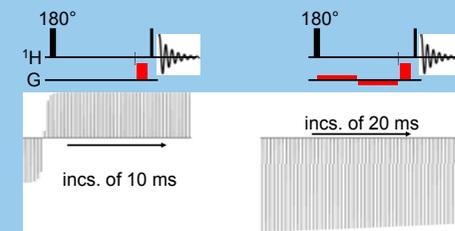
1. G<sub>4</sub> and G<sub>5</sub> dephase recovered water
2. final pulse flips recovered water onto z

4-54

### Radiation damping

- transverse magnetization induces a B<sub>1</sub> field in the coil; this field rotates the magnetization towards +z
- effect is significant for large signals (water), high fields and high 'Q' probes
- water may return from transverse to +z in a few ms; also from -z (slower)

### Controlling radiation damping



Weak dephase/rephase gradient prevents build up of transverse magnetization

## Zero-quantum dephasing

## An old, old problem in NMR

z-magnetisation and zero-quantum coherence cannot be separated using phase cycling or gradients

*because*  
neither respond to z-rotations

i.e. both have coherence order,  $p$ , of zero

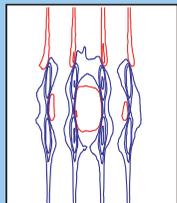
## Why is it a problem?

a  $90^\circ$  pulse converts z-magnetization into **in-phase** magnetization along  $y$

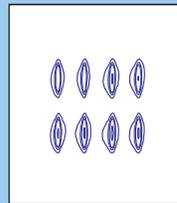
*but* converts ZQ into **anti-phase** along  $x$

the result is **phase distortion** and **unwanted peaks**

## Result: distorted multiplets in 2D

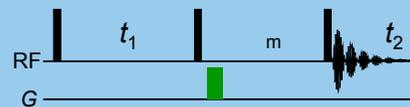


z-magn. + ZQ



z-magn. only

## Example: NOESY

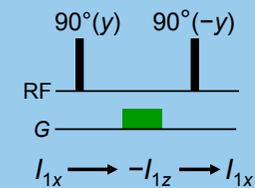


wanted: z-magn. during  $m$   
→ in-phase, absorption multiplets

**unwanted:** ZQ during  $m$   
→ anti-phase, dispersion multiplets  
'J-peaks'

## The z-filter

Sørensen, Rance, Ernst 1984



everything else → **dephased**

**only in-phase magnetization survives**

**but ...**

$2I_{1y}I_{2z} \rightarrow 2I_{1y}I_{2x}$  mixture of DQ and ZQ  
 $\rightarrow \frac{1}{2}(2I_{1y}I_{2x} - 2I_{1x}I_{2y}) \rightarrow \frac{1}{2}(2I_{1y}I_{2z} - 2I_{1z}I_{2y})$   
 ZQ

**Anti-phase component passes through**

**Zero-quantum evolution**

The zero quantum evolves during  $\tau_z$  at  $(\Omega_1 - \Omega_2)$ , the difference of the shifts

*Macura et al 1981* **this is the key ...**

**Make evolution dependent on position**

**frequency**

**position**

**Zero-quantum dephasing**

As frequency is a **function of position**, the zero-quantum coherence will **dephase**

Identical to dephasing in a conventional gradient

**how to make 180° position dependent?**

**Swept-frequency 180°**

normal spectrum  
 apply gradient  
 frequency position  
 swept-frequency 180° pulse

**different parts experience pulse at different times**

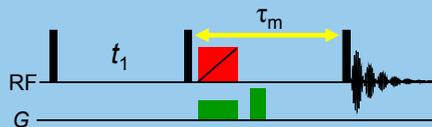
**z-filter with zero-quantum suppression**

swept 180° with gradient  
 additional dephasing gradient (to make sure everything is dephased)

### Typical parameters

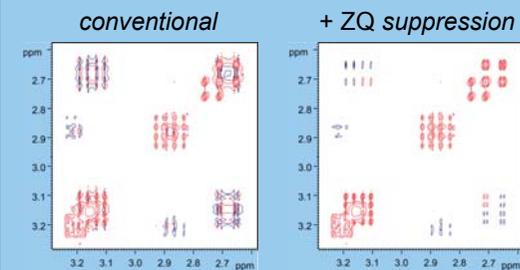
- swept pulse of duration 15 to 30 ms
- gradient 1 to 2 G cm<sup>-1</sup>
- dephasing rate depends on ZQ frequency
- suppression of ZQ by factor of 100

### NOESY with zero-quantum suppression



swept 180° with gradient  
 additional dephasing gradient  
 NOE continues to build up throughout

### NOESY results (strychnine)

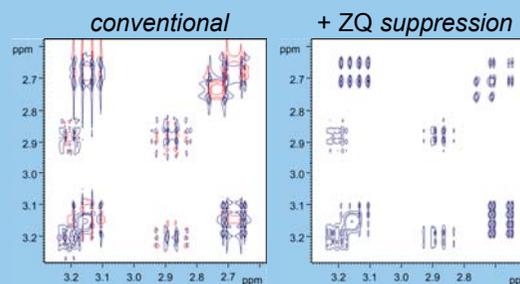


### TOCSY

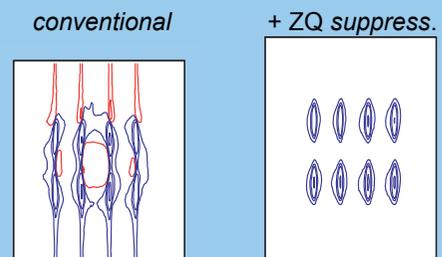


isotropic mixing within z-filter  
 ZQ dephasing needed before and after mixing; unequal durations

### TOCSY results (strychnine)



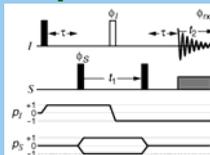
### TOCSY results (strychnine)



### Advantages of the z-filter

- excellent suppression
- no increase in experiment time
- simple to implement
- widely applicable
- negligible reduction in signal

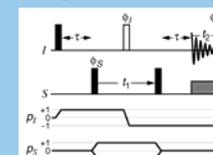
### Examples: HMQC



select  $\Delta p_S = \pm 1$  at first S pulse  
and  $\Delta p_I = \pm 2$  at  $180^\circ$  I pulse

step	1	2	3	4	5	6	7	8
$\phi_S$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$	$0^\circ$	$180^\circ$
$\phi_I$	$0^\circ$	$0^\circ$	$90^\circ$	$90^\circ$	$180^\circ$	$180^\circ$	$270^\circ$	$270^\circ$
$\phi_{Ix}$	$0^\circ$	$180^\circ$	$180^\circ$	$0^\circ$	$0^\circ$	$180^\circ$	$180^\circ$	$0^\circ$

### Difference spectroscopy: HMQC



The cycle  $[0^\circ, 180^\circ]$  on first S pulse and rx. is just **difference spectroscopy**:  
selects that part of the signal which goes via the S spin

### Difference spectroscopy

In heteronuclear experiments, a simple two-step phase cycle (+x/-x) on the pulse causing the transfer often suffices

- this is simply difference spectroscopy